

# 11-Maximum Power Point Tracking

ECEGR 452  
Renewable Energy Systems



# Overview

- PV Applications
- Maximum Power Point
- Boost Converter
- Illustrative Simulation

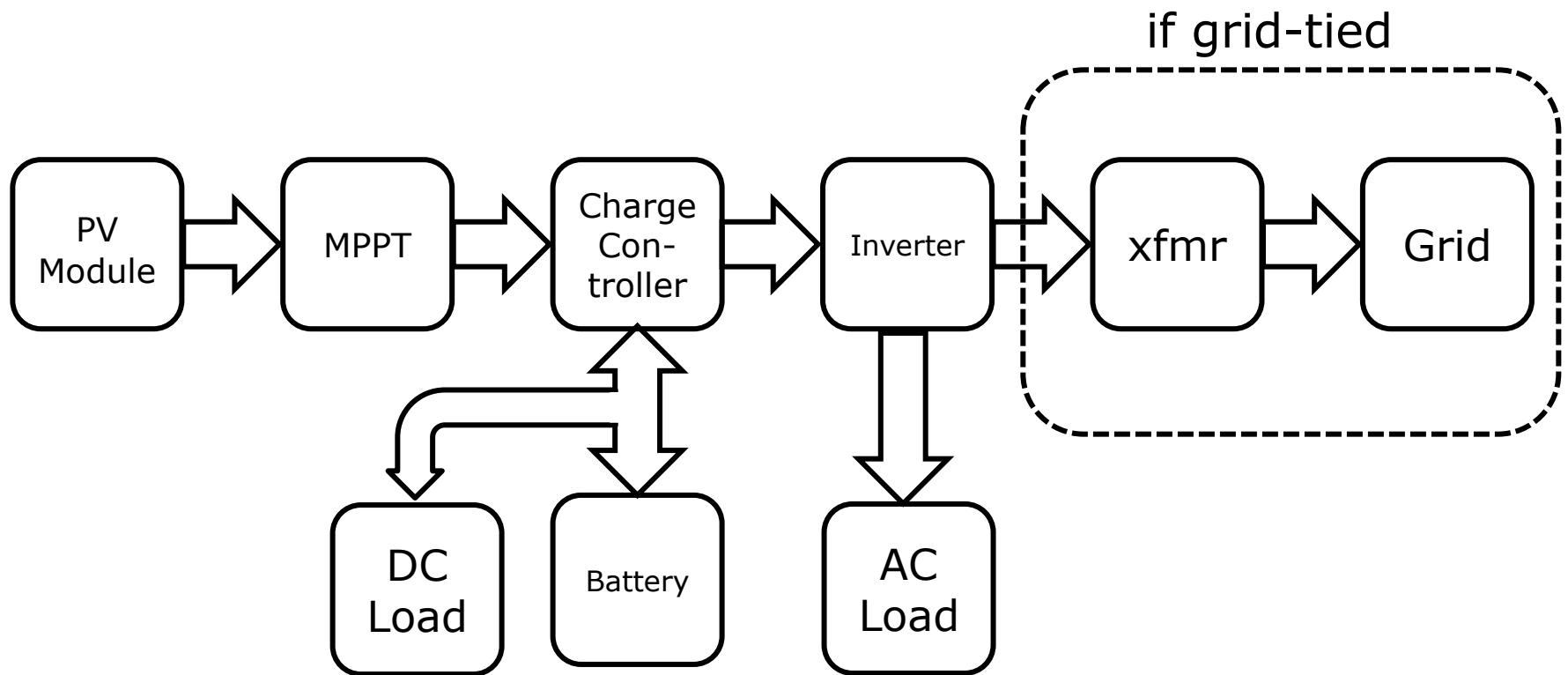


# PV Applications

- Stand-Alone: all energy supplied to load originates from PV
  - remote applications
- Grid Connected: energy from PV may serve local load or be exported to the electric grid. Import of energy from the grid possible
  - PV power plants
  - urban applications
- Hybrid: PV + one or more generation sources (such as diesel generator), may be connected to the grid



# Common PV System Elements





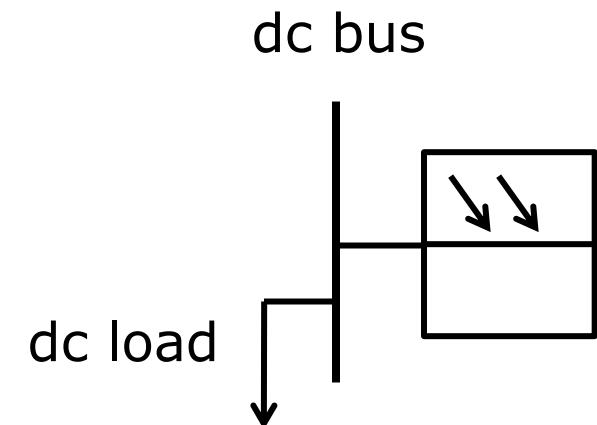
# PV System Elements

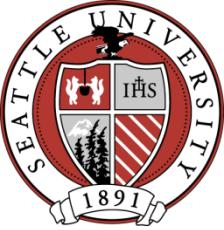
- Generation
  - PV module(s)
  - diesel
  - other
- Power electronic converters
  - DC/AC (inverters)
  - DC/DC (buck, boost, buck boost)
- Load
  - AC
  - DC
- Storage
  - battery
  - hydrogen
- Transformer



# Stand Alone PV System

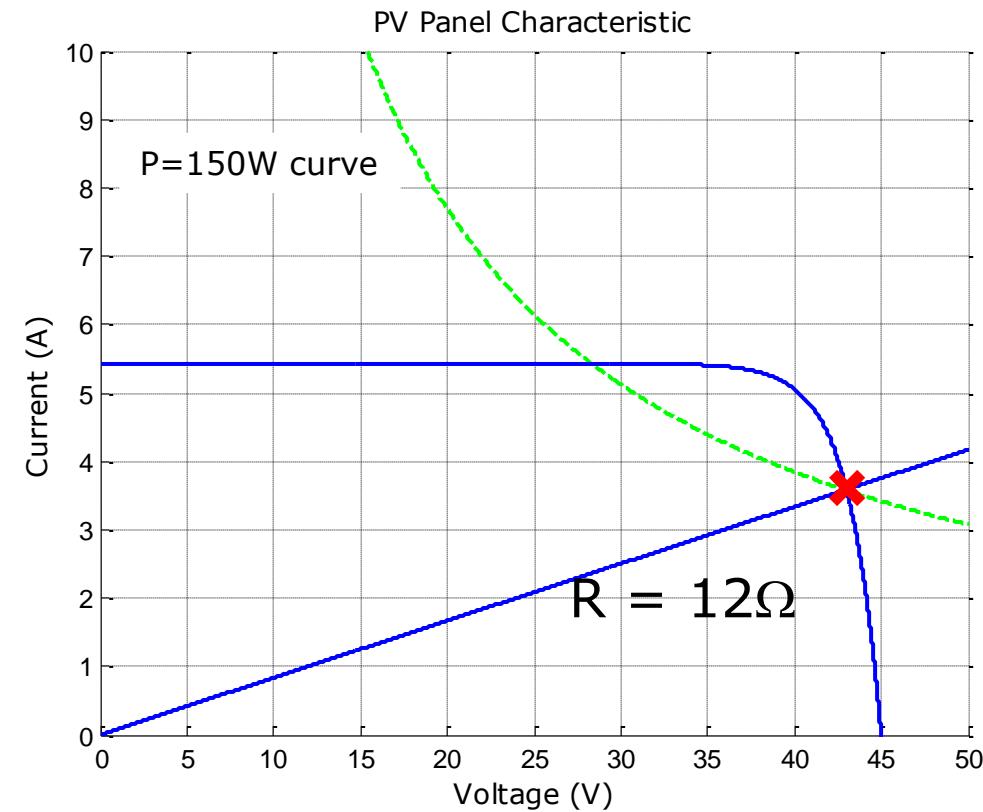
- Simple dc system
  - one PV module
  - one 12 Ohm resistive load (a heater)





# Stand Alone PV System

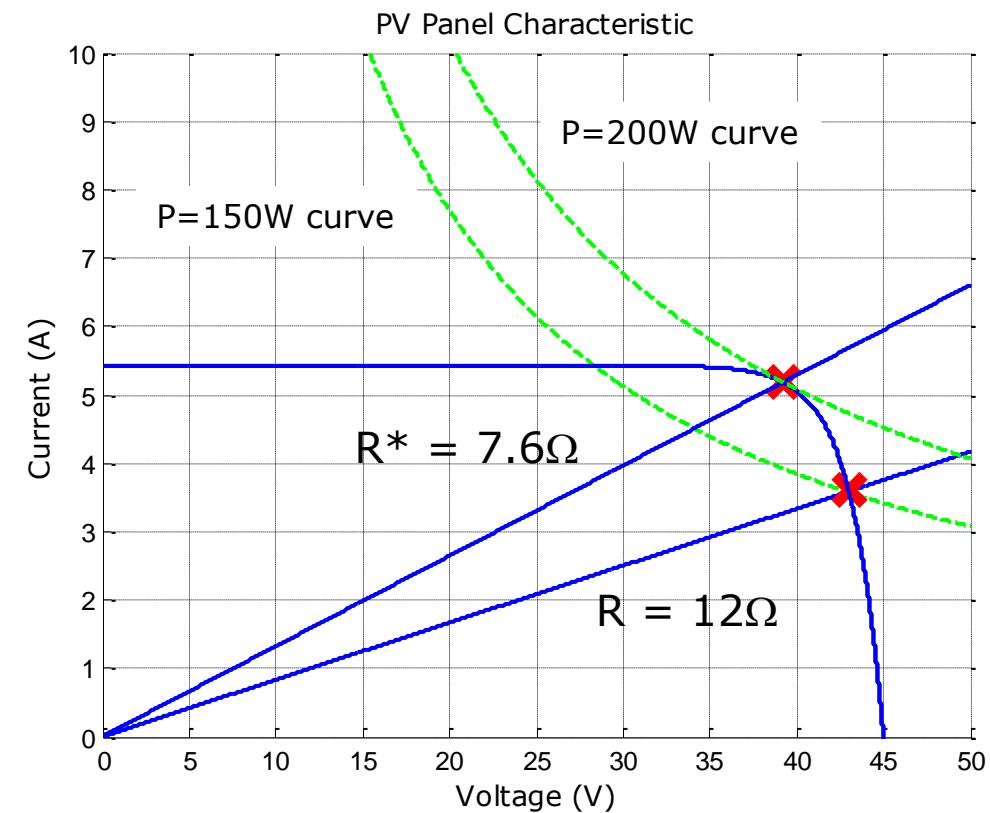
- With 12 Ohm load
  - $P = 150 \text{ W}$
- Module Characteristics
  - $P^* = 200 \text{ W}$
  - Power output is not maximized

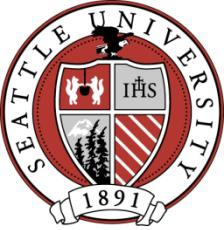




# Stand Alone PV System

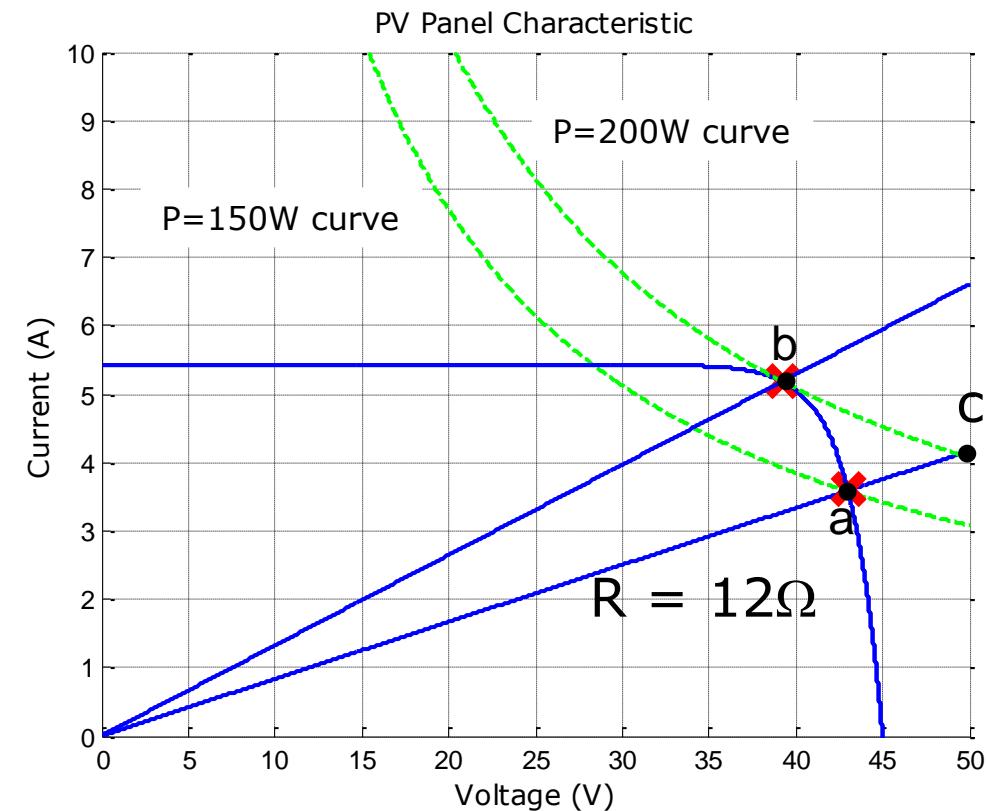
- At optimal operating point  $R = 7.6\Omega$





# Stand Alone PV System

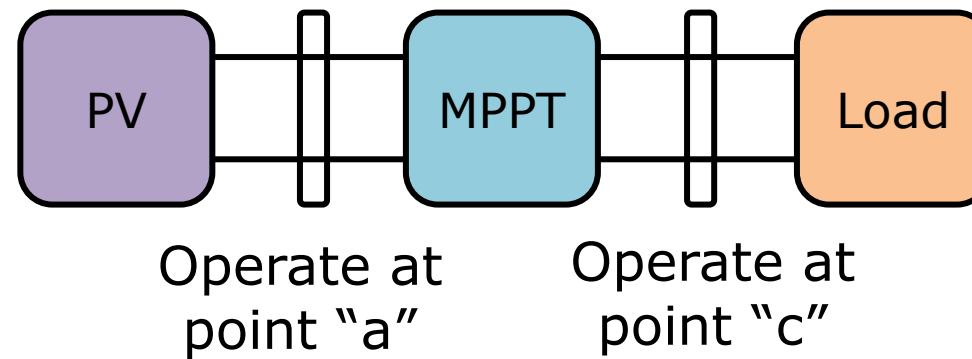
- Need to “move” operating point of the PV from a to b
- Need to move operating point of the load from a to c (increase voltage)
- Need an interface between PV panel and load





# Maximum Power Point Trackers

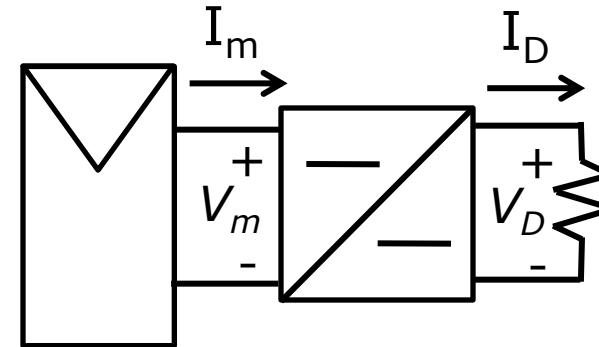
- Use Maximum Power Point Tracker (MPPT): dc-dc converter
- HOMER assumes that the design has a MPPT in the converter





# Maximum Power Trackers

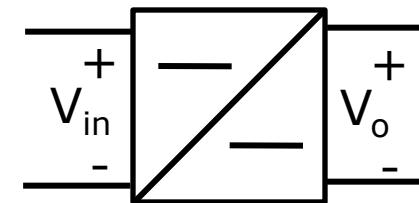
- DC-DC converter
  - controls output voltage
  - ideal (no losses)
  - power is conserved  $(V_m \times I_m) = (V_D \times I_D)$

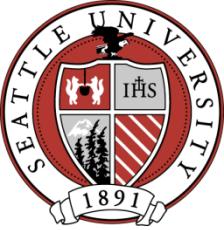




# Maximum Power Trackers

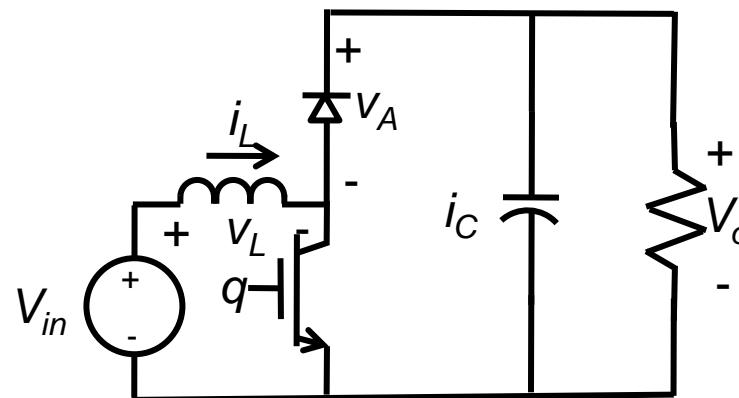
- In most cases, the voltage at the load must be greater than the PV module voltage for maximum power transfer
- Voltage must be “boosted”
  - $V_o > V_{in}$
- Use a Boost Converter





# Boost Converter

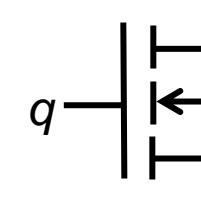
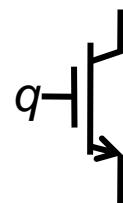
- Used to efficiently produce output voltage that is **greater** than input voltage
- First analyze assuming input is a voltage source

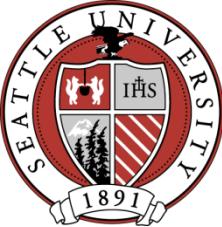




# Boost Converter

- Power electronic components
  - IGBT (Insulated Gate Bipolar Transistor)
  - MOSFETs
- Behave like controllable switches
  - $q = 1$ ; switch is closed
  - $q = 0$ ; switch is open





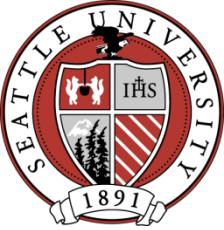
# Inductor Model

- Recall:
  - L: inductance (H)
  - current through inductors cannot change instantaneously
- Behavior is described as:

$$v_L = L \frac{di}{dt} \Rightarrow i_L(t) = \frac{1}{L} \int_{\tau}^t v_L d\tau$$

$$i_L(t) = i_L(0) + \frac{1}{L} \int_0^t v_L d\tau$$

$$E = \frac{1}{2} L i_L^2$$

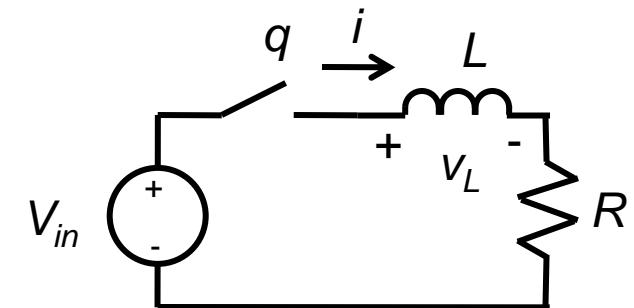


# Inductor Model

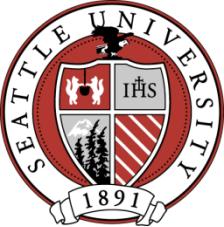
- Switch q closes at  $t = 0$
- Response of the circuit is computed as

$$V_{in} = Ri + L \frac{di}{dt}$$

$$\frac{di}{dt} = \frac{V_{in} - Ri}{L} = \frac{-R}{L} \left( i - \frac{V_{in}}{R} \right)$$



$$L = 100\mu\text{H}, V_{in} = 10 \text{ V}, R = 5\Omega$$



# Inductor Model

$$V_{in} = Ri + L \frac{di}{dt}$$

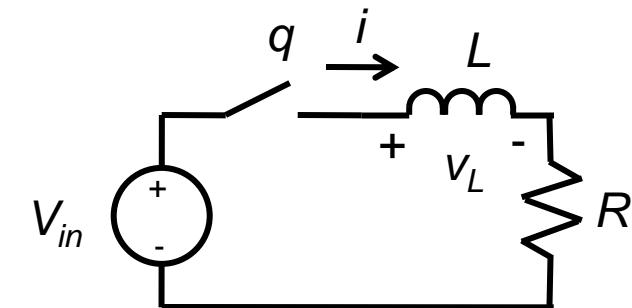
$$\frac{di}{dt} = \frac{V_{in} - Ri}{L} = \frac{-R}{L} \left( i - \frac{V_{in}}{R} \right)$$

- Solving the differential equation gives:

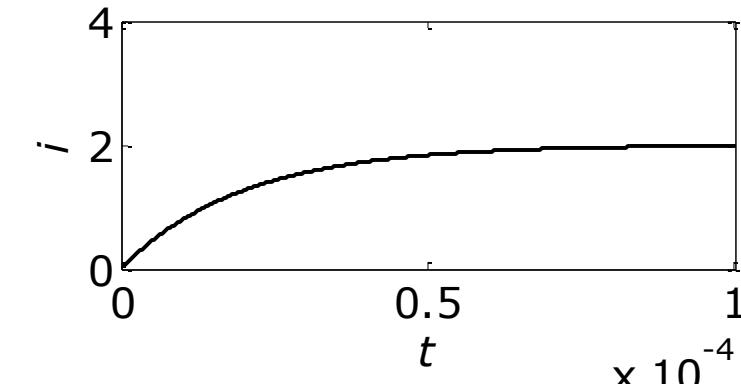
$$i(t) = \frac{V_{in}}{R} - \frac{V_{in}}{R} e^{-(R/L)t}$$

time constant  $L/R$

- Note the dependence of the time constant,  $\tau$ , on  $L$  and  $R$



$$L = 100\mu\text{H}, V_{in} = 10 \text{ V}, R = 5\Omega$$



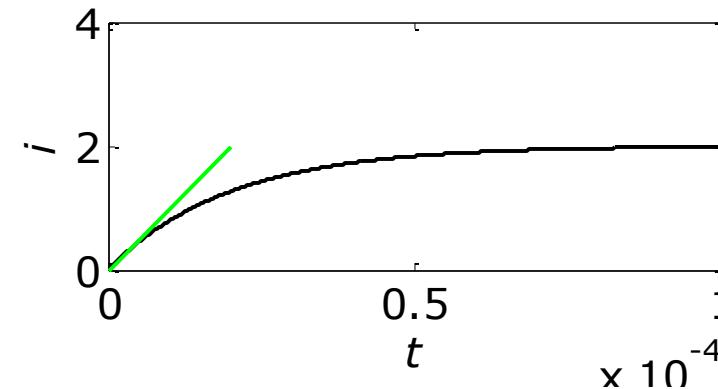


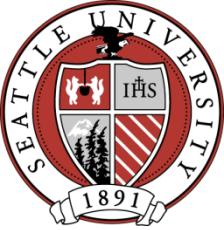
# Response of R-L Circuit

- If we are only interested in  $t < \tau$ , then we can use a linear approximation

$$v_L = L \frac{\Delta i}{\Delta t}$$

- We will use linear approx. hereafter (fast switching time, large inductances)

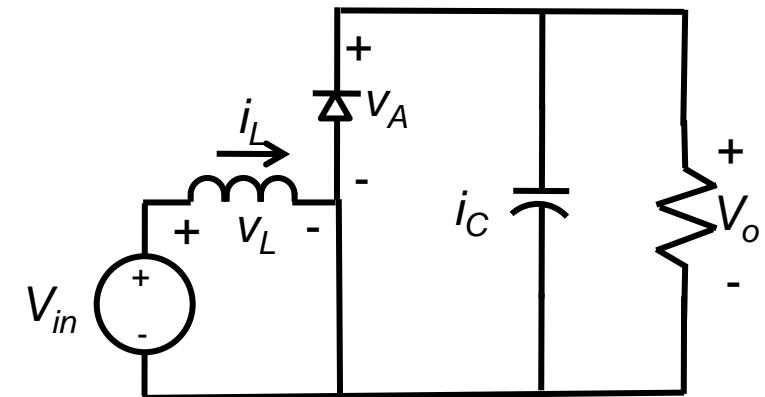
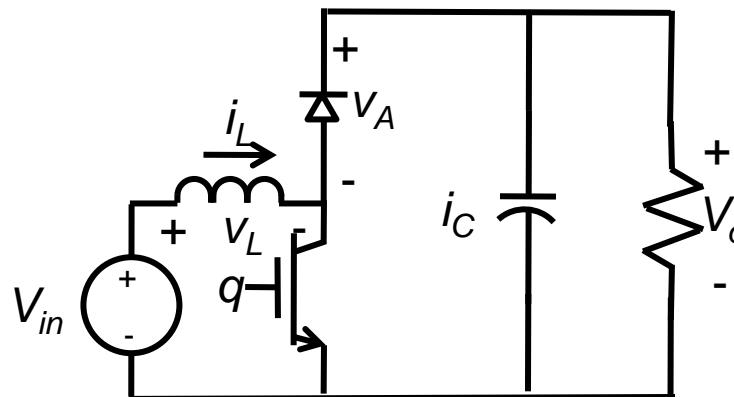




# Boost Converter

- Assume  $q = 1$
- transistor is in the on-state
- Is the diode conducting?

(switch closed)





# Boost Converter ( $q=1$ )

- Diode is in the off-state

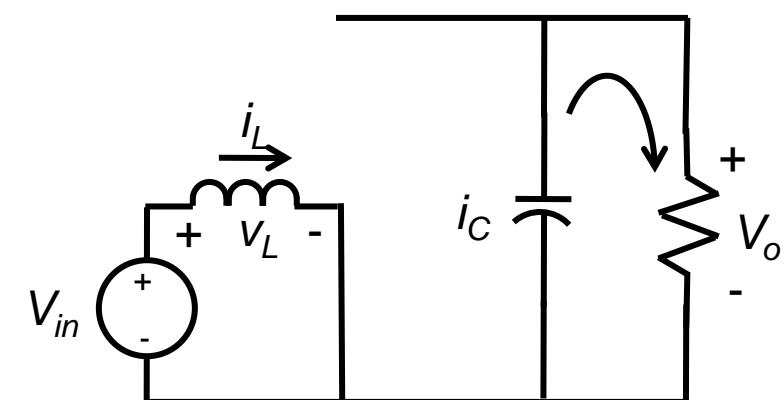
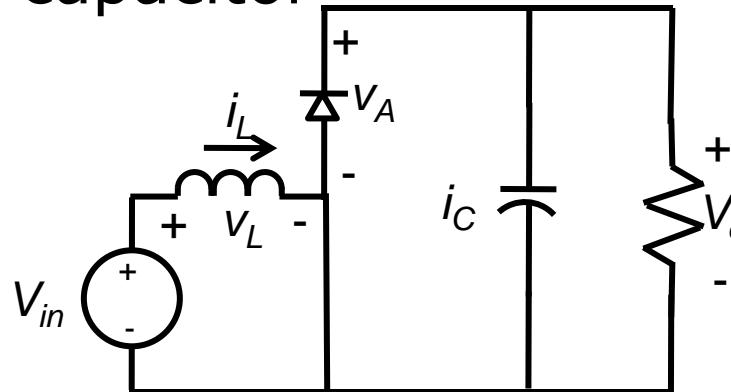
$$v_A = v_o > 0$$

- Observations

$$v_L = V_{in}$$

$$i_{in} = i_L$$

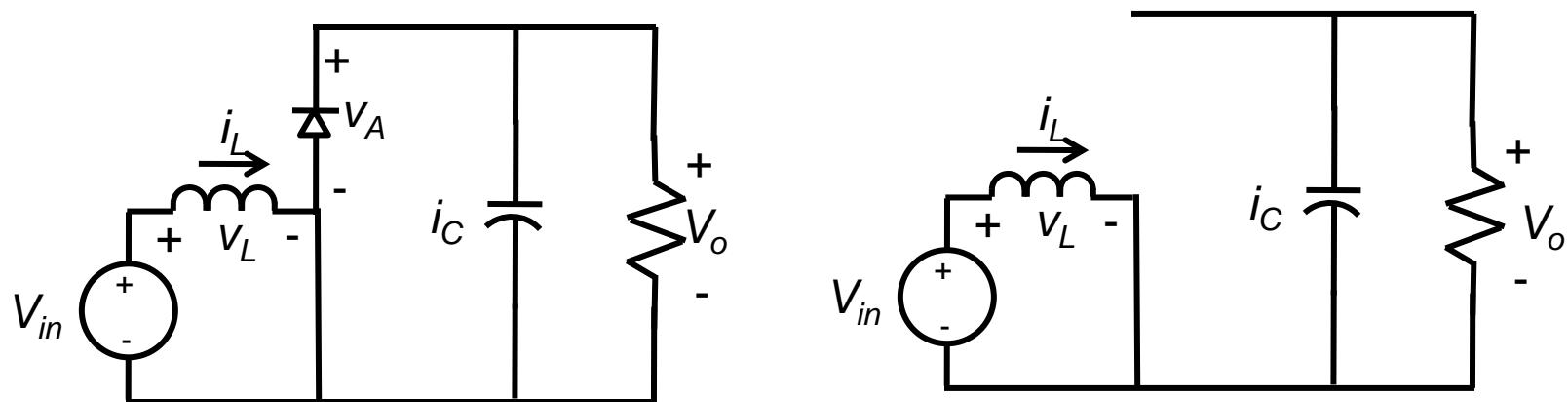
- Load current is supplied by discharging the capacitor





# Boost Converter ( $q=1$ )

- Voltage across inductor is positive
  - Inductor current increases (assumed linear)

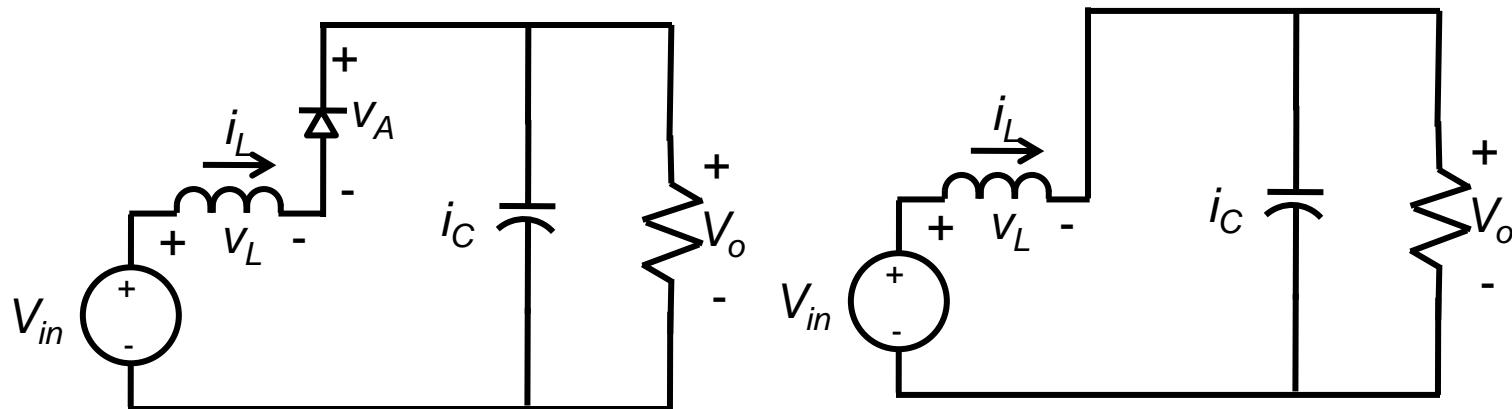




# Boost Converter ( $q=0$ )

- Now assume  $q = 0$
- Transistor is in the off-state
- Is the diode conducting?
  - diode is in the on-state (inductor current must flow)

(switch open)





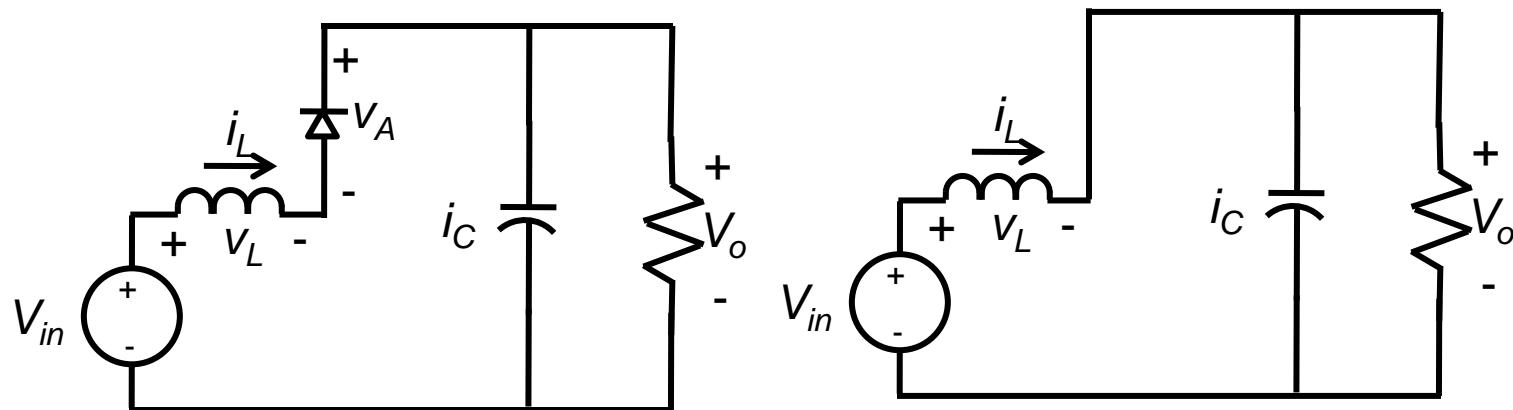
# Boost Converter ( $q=0$ )

- Observations

$$v_L = V_{in} - V_o \quad (\text{ignoring diode voltage drop})$$

$$i_{in} = i_L$$

- If  $V_o > V_{in}$ , then  $V_L$  is negative
  - inductor current decreases (assumed linear)





# Boost Converter Inductor Voltage

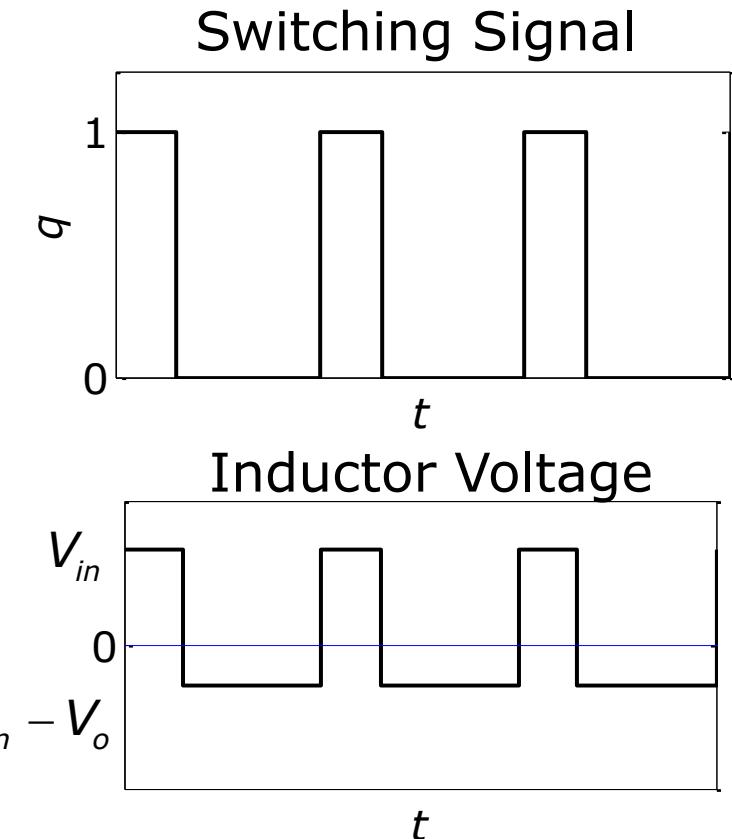
- If  $q = 1$ , then

$$V_L = V_{in}$$

- If  $q = 0$ , then

$$V_L = V_{in} - V_o$$

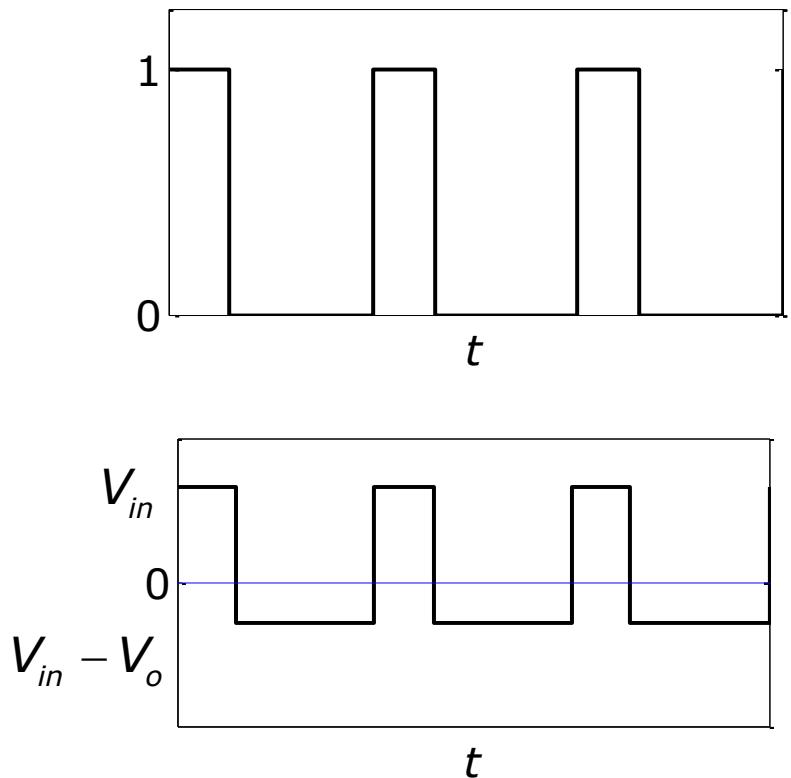
- What is the average output voltage?





# Boost Converter Inductor Voltage

- What is the average output voltage?
  - average inductor voltage must equal zero
  - otherwise the current (and energy) increases





# Boost Converter Inductor Voltage

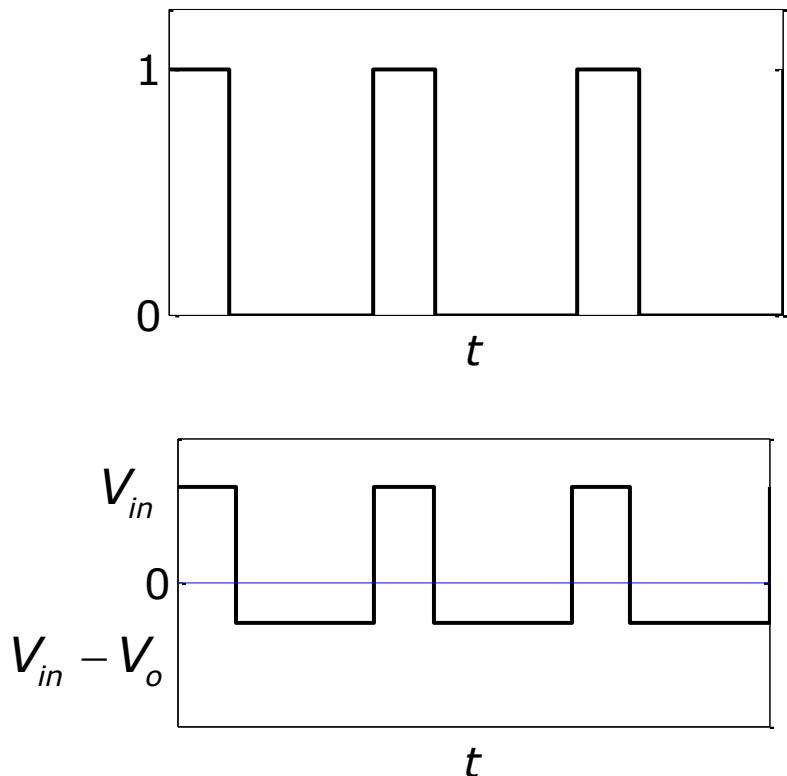
- Let the duty ratio D be the percent of time that  $q = 1$
- Then:

$$D(V_{in}) + (1 - D)(V_{in} - V_o) = 0$$

$$\Rightarrow DV_{in} + V_{in} - V_o - DV_{in} + DV_o = 0$$

$$\Rightarrow V_o(-1 + D) + V_{in}(D + 1 - D) = 0$$

$$\Rightarrow V_o = \frac{1}{1 - D} V_{in} \text{ important result!}$$





# Boost Converter Inductor Current

- If  $v_L > 0$ , then

$$\Delta i_{L, \text{pos}} = \frac{1}{L} (V_{in}) D T_s$$

- If  $v_L < 0$ , then

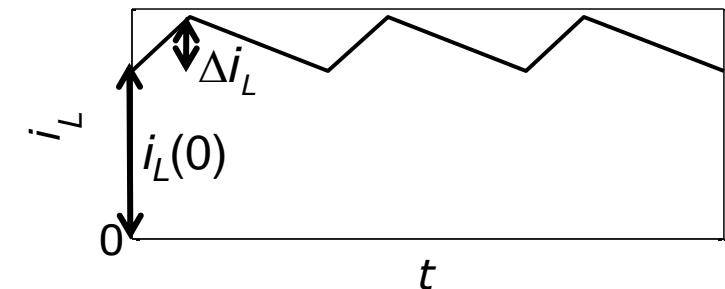
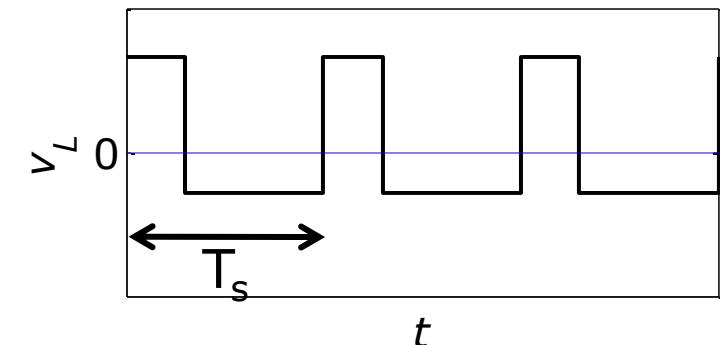
$$\Delta i_{L, \text{neg}} = -\frac{1}{L} (V_o - V_{in}) (1 - D) T_s$$

- and

$$\Delta i_L = \Delta i_{L, \text{pos}} = \Delta i_{L, \text{neg}}$$

- Average inductor current:

$$I_L = I_{in} = \frac{V_o}{V_{in}} I_o = \frac{1}{1 - D} \left( \frac{V_o}{R} \right)$$





# Boost Converter Input Current

- If  $q = 1$ , then

$$i_{in} = i_L$$

- If  $q = 0$ , then

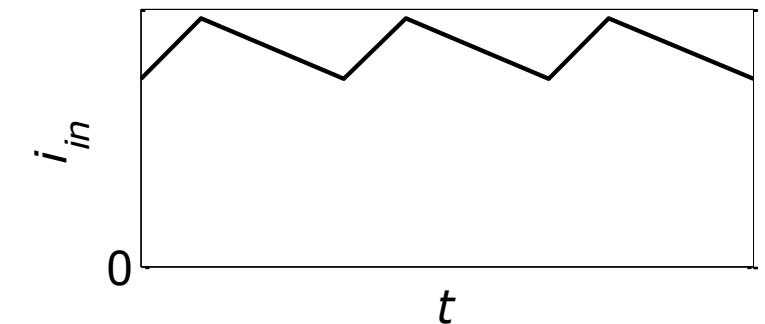
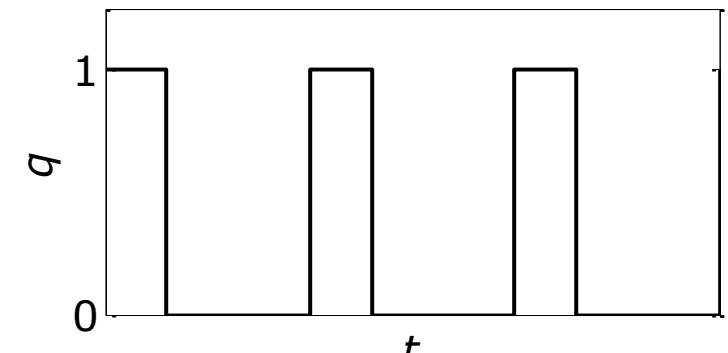
$$i_{in} = i_L$$

- Average input current is

$$I_{in} = I_L$$

- Power in equals power out

$$V_{in}I_{in} = V_oI_o$$





# Boost Converter Capacitor Current

- If  $q = 1$ , then

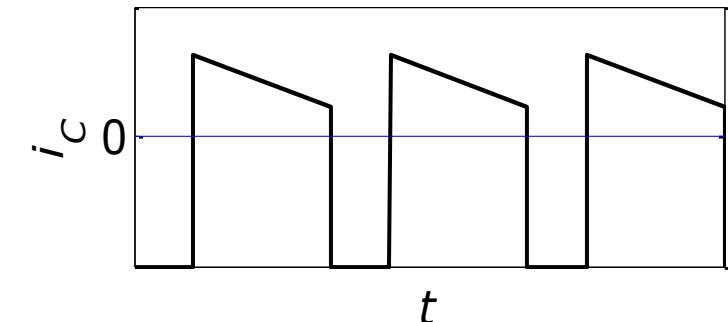
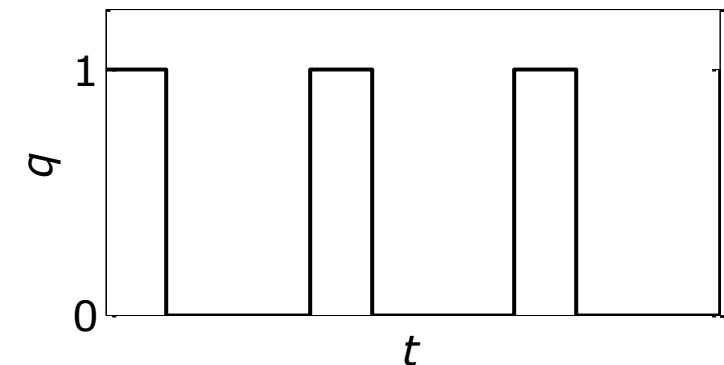
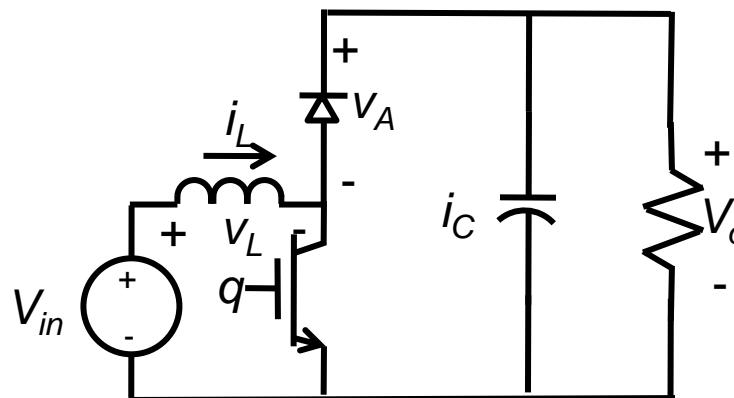
$$i_c = -I_o$$

- If  $q = 0$ , then

$$i_c = i_{rip}$$

- Output voltage has ripple

$$\Delta V_o = \frac{i_c \Delta t}{C}$$





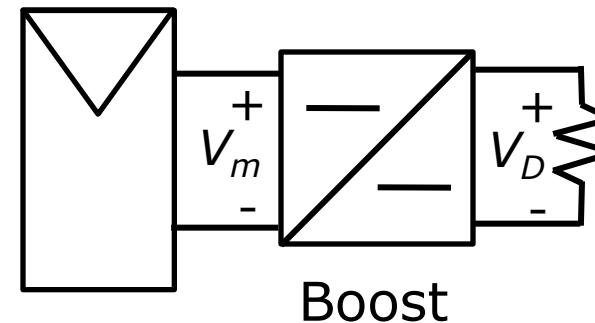
# Boost Converter Capacitor Current

- Must find D that maximizes the power output

$$V_o = \frac{1}{1-D} V_{in}$$

$$D = 1 - \frac{V_{in}}{V_o}$$

- $V_{in}$  is not a voltage source, so D cannot be made arbitrarily large





# Maximum Power Trackers

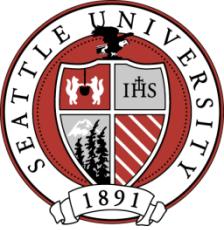
- What should the voltage at the load be to ensure maximum power transfer?

$$P^* = V^* I^* \quad \text{Recall: } P^* \text{ is the maximum power under the given conditions}$$

$$P_D = V_D I_D = \frac{V_D^2}{R} = P^*$$

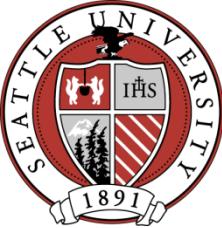
$$V_D^* = \sqrt{P^* R}$$

- Therefore:  $D = 1 - \frac{V_{STC}^*}{V_D^*} = 1 - \frac{V_{STC}^*}{\sqrt{P^* R}}$
- The duty ratio should not exceed this value



# Maximum Power Trackers

- Find D of a boost MPPT if:
  - load resistance is 12 Ohms
  - $V^* = 38 \text{ V}$
  - $P^* = 200 \text{ W}$



# Maximum Power Trackers

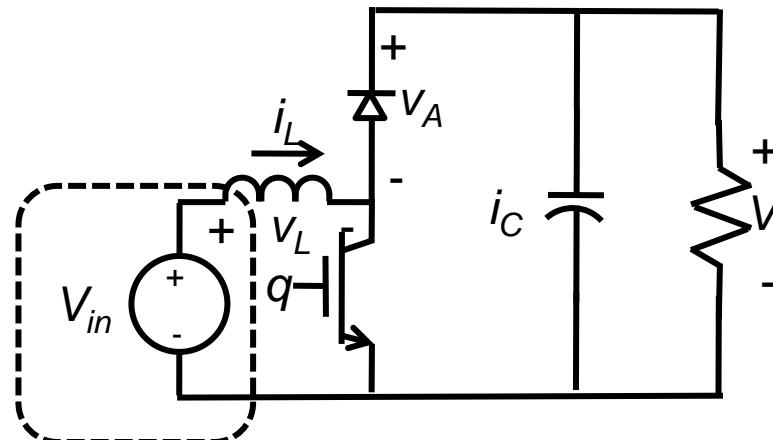
- Find D of a boost MPPT if:
  - load resistance is 12 Ohms
  - $V^* = 38 \text{ V}$
  - $P^* = 200 \text{ W}$

$$D = 1 - \frac{V^*}{V_D^*} = 1 - \frac{V^*}{\sqrt{P^* R}} = 0.224$$

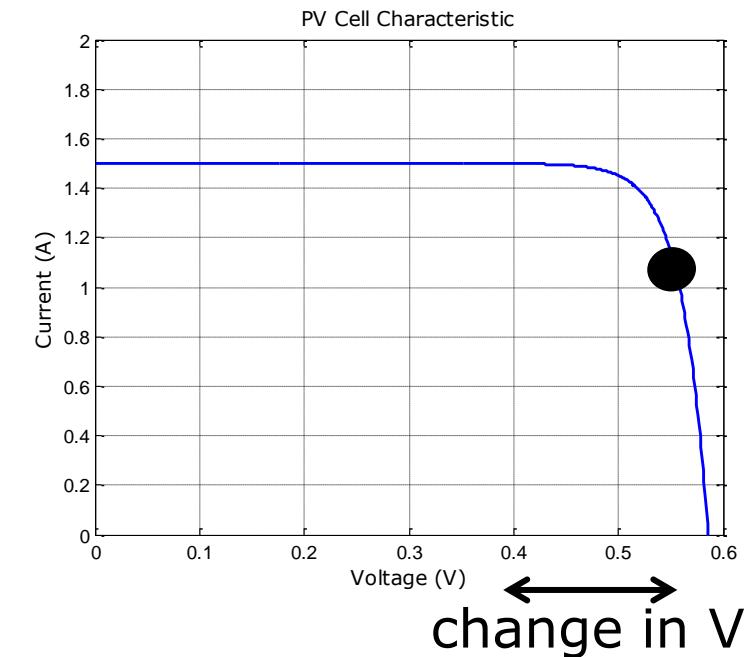


# Maximum Power Trackers

- Note: PV panels cannot be modeled as independent voltage sources
  - As  $I_{in}$  increases, the voltage decreases



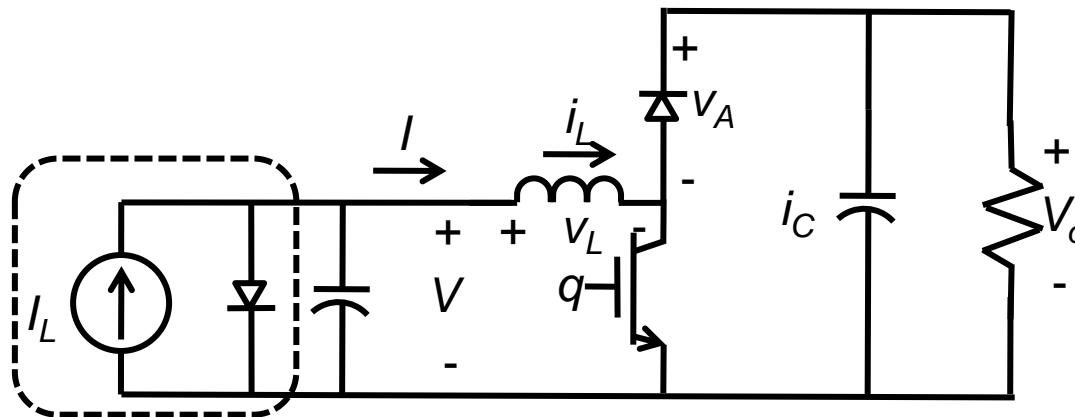
Inappropriate PV model

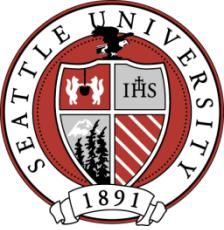




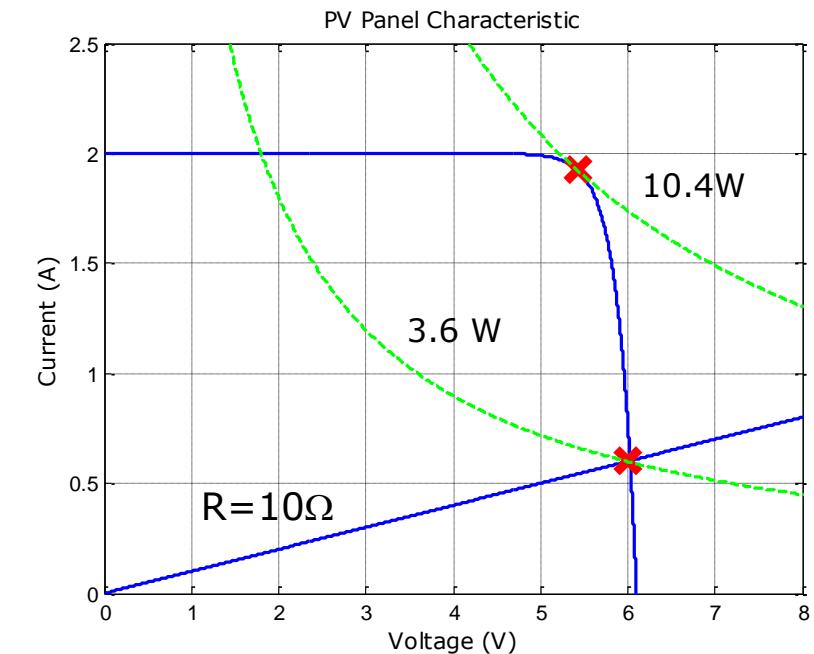
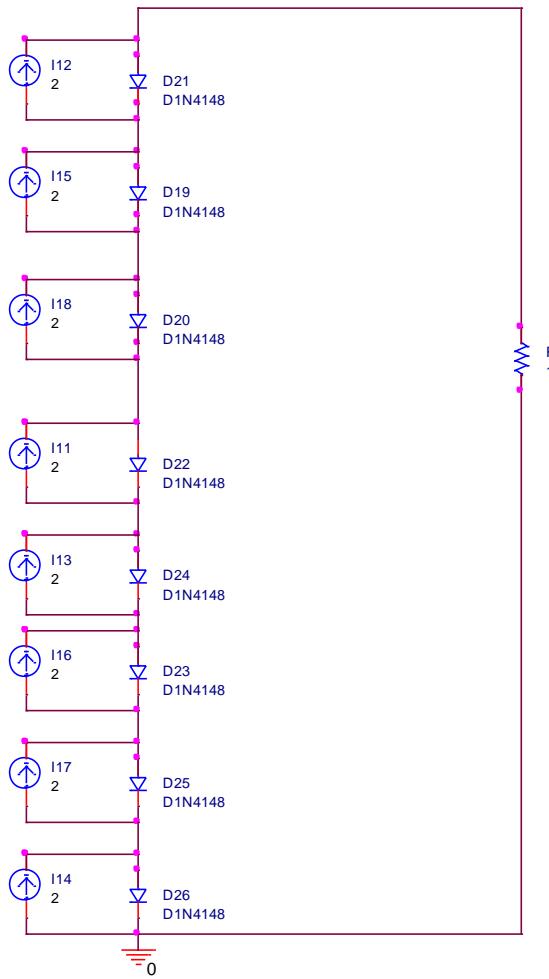
# Maximum Power Trackers

- Include input capacitor to steady voltage





# Maximum Power Trackers



$$D = 1 - \frac{V_{STC}^*}{\sqrt{P_{STC}^* R}} = 1 - \frac{5.42}{\sqrt{10.4 \times 2.8}} = 0.47$$



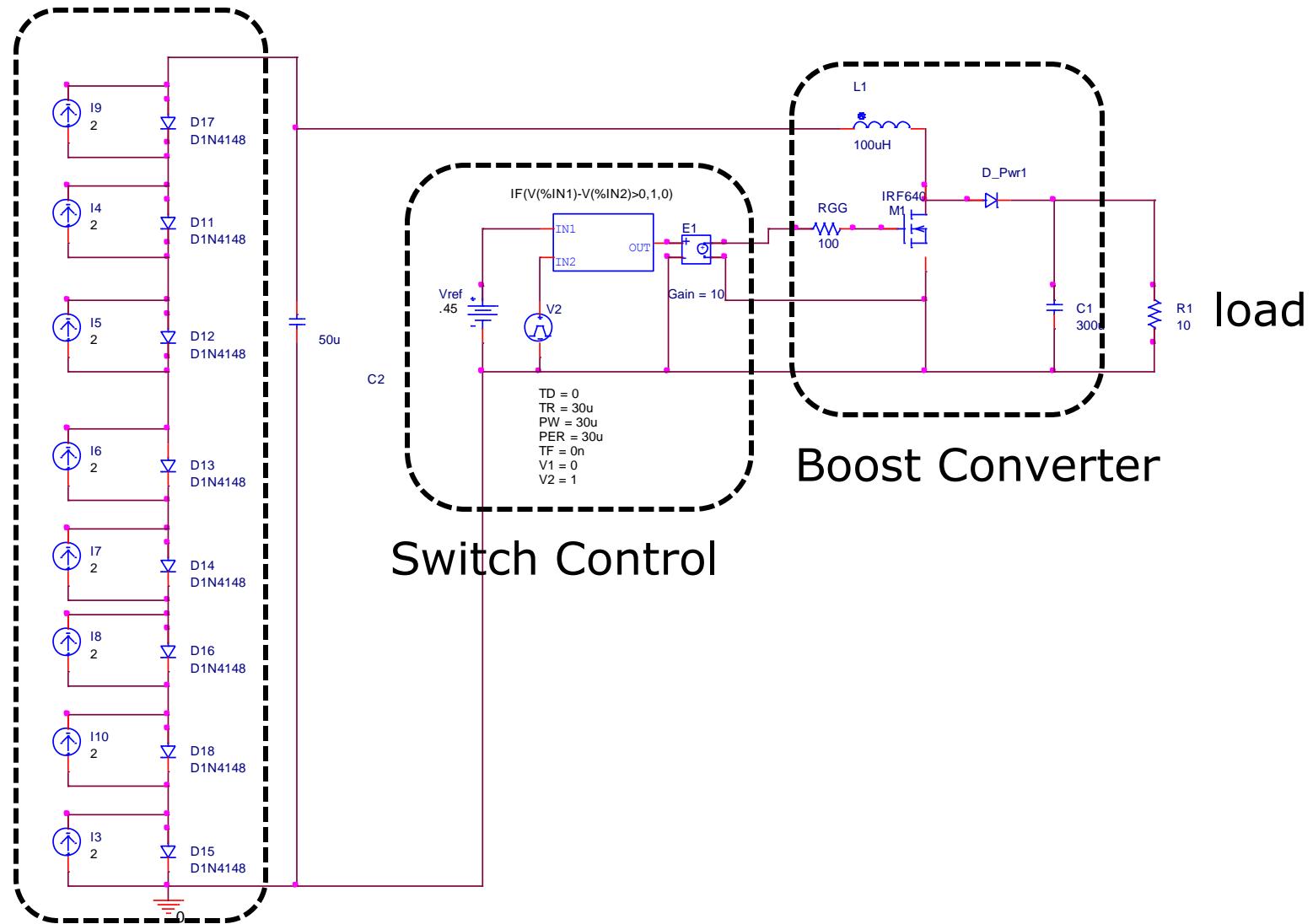
# Maximum Power Trackers





# Maximum Power Trackers

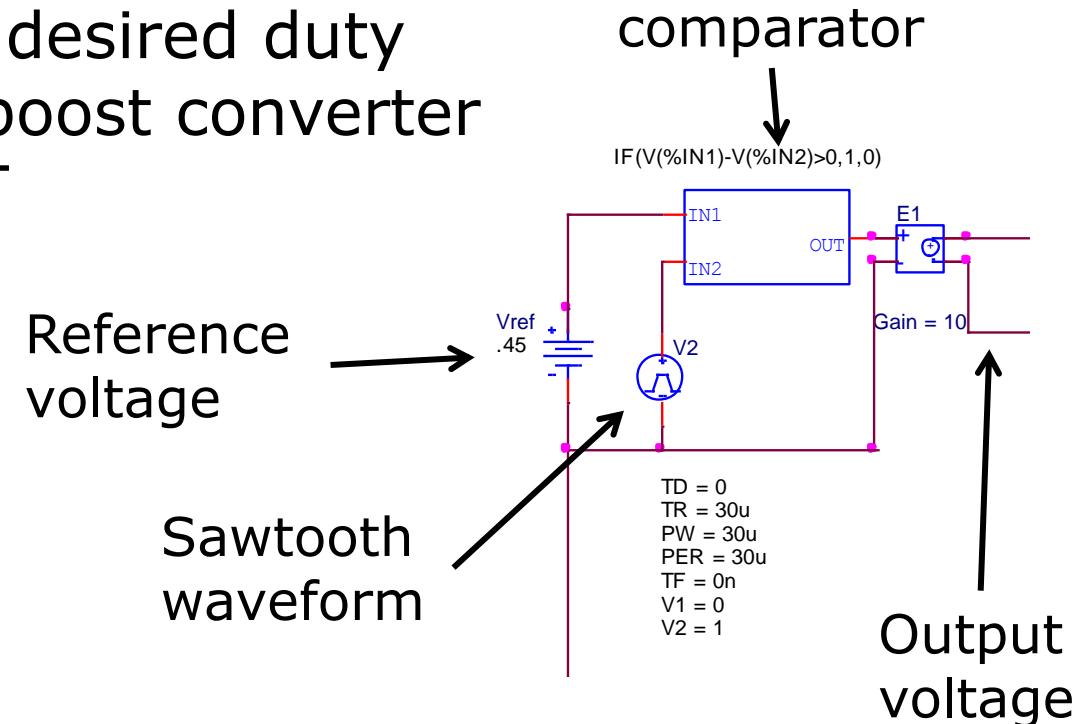
PV  
Module

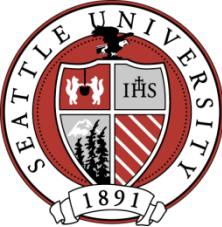




# Switch Control

- Function: output square voltage wave of desired duty ratio to control boost converter MOSFET or IGBT



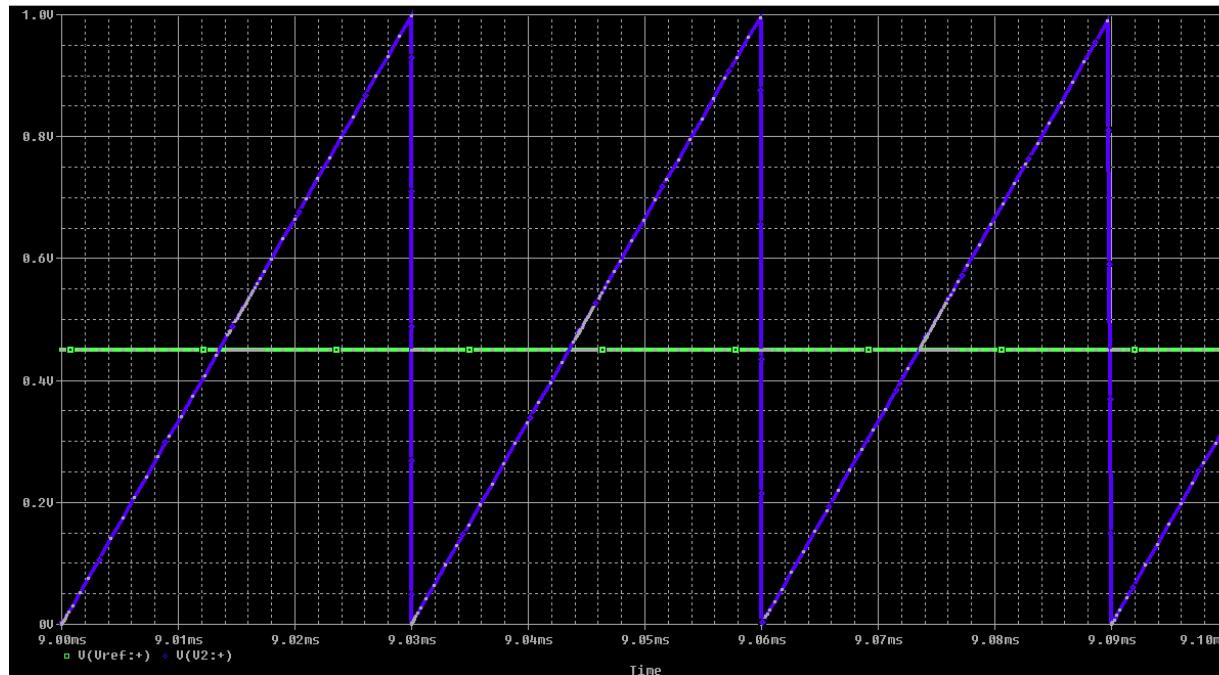


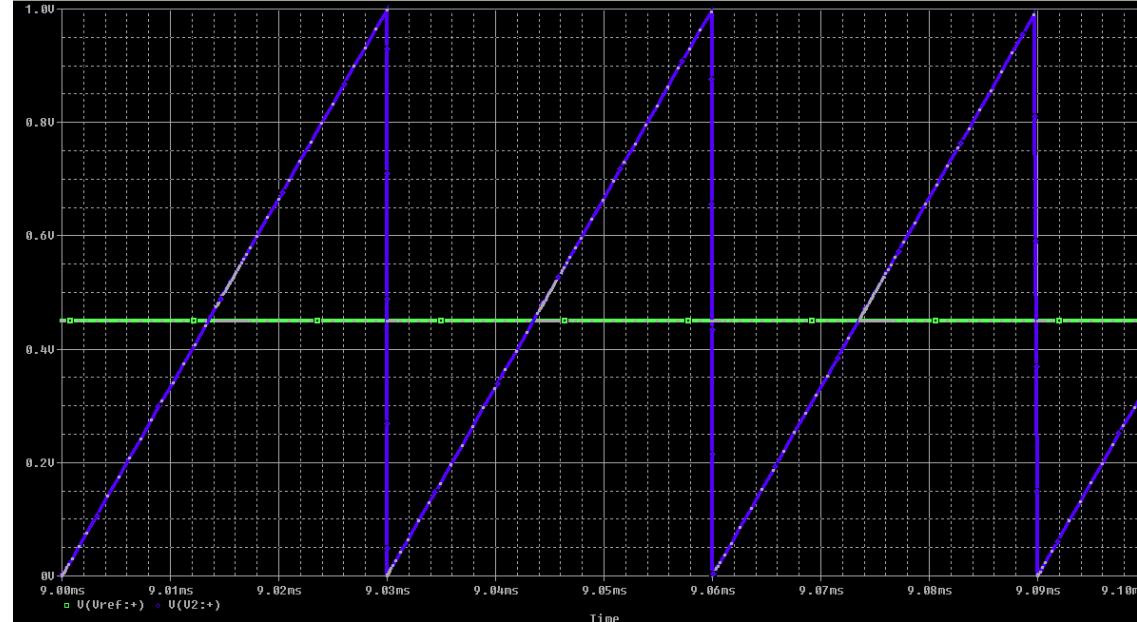
# Switch Control

Set reference voltage to desired duty ratio

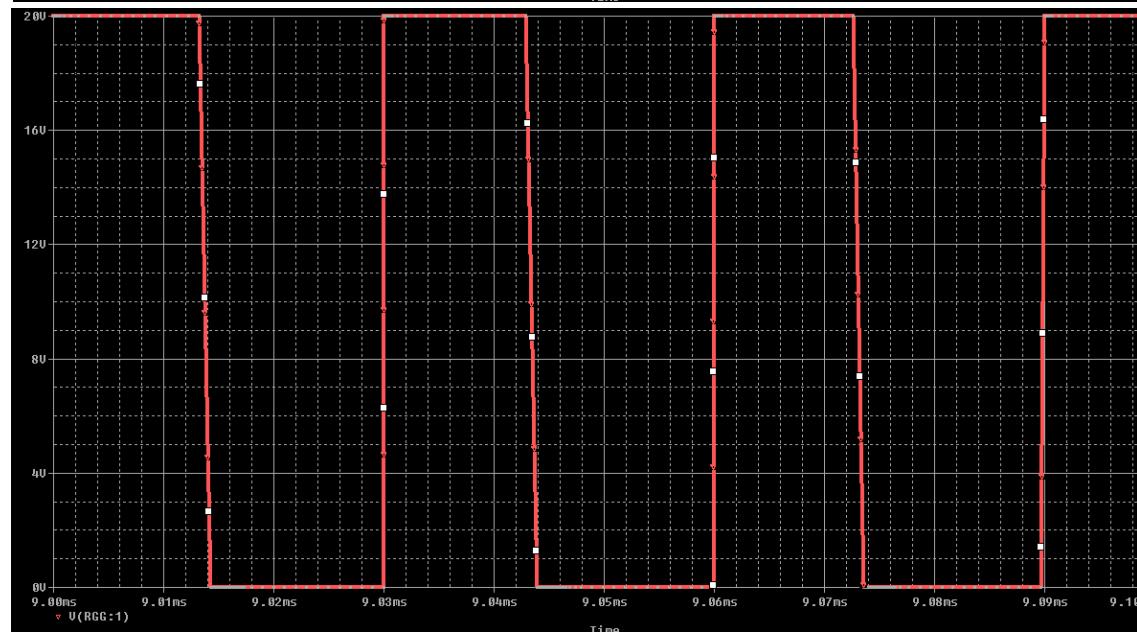
If  $V_{ref} > V_{saw}$ ,  $q = 1$

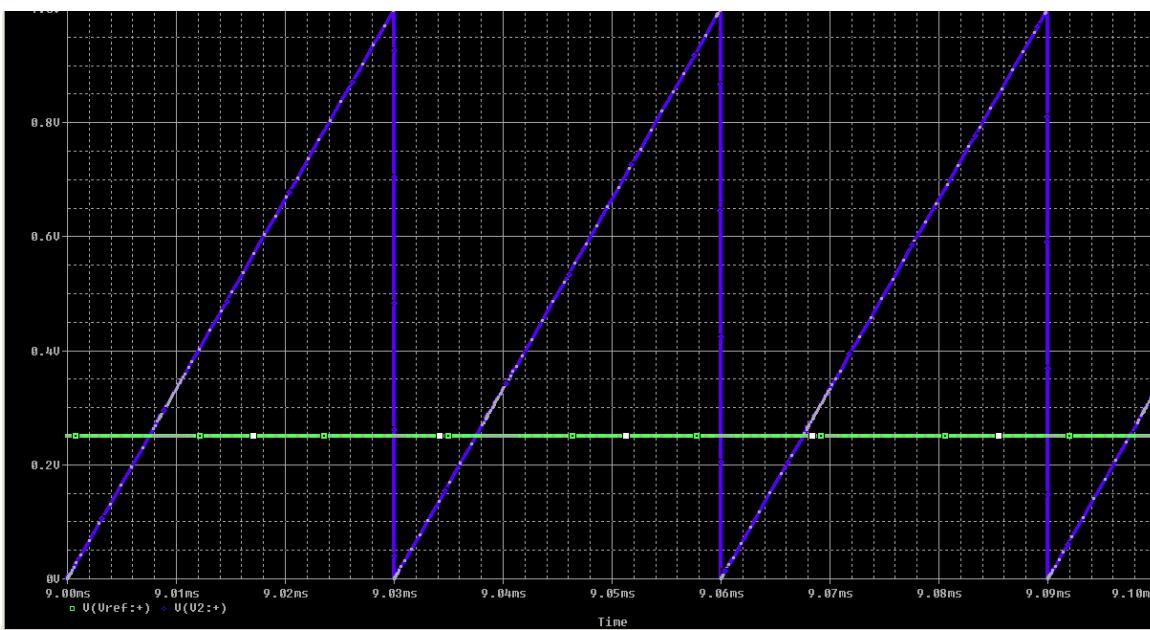
else,  $q = 0$



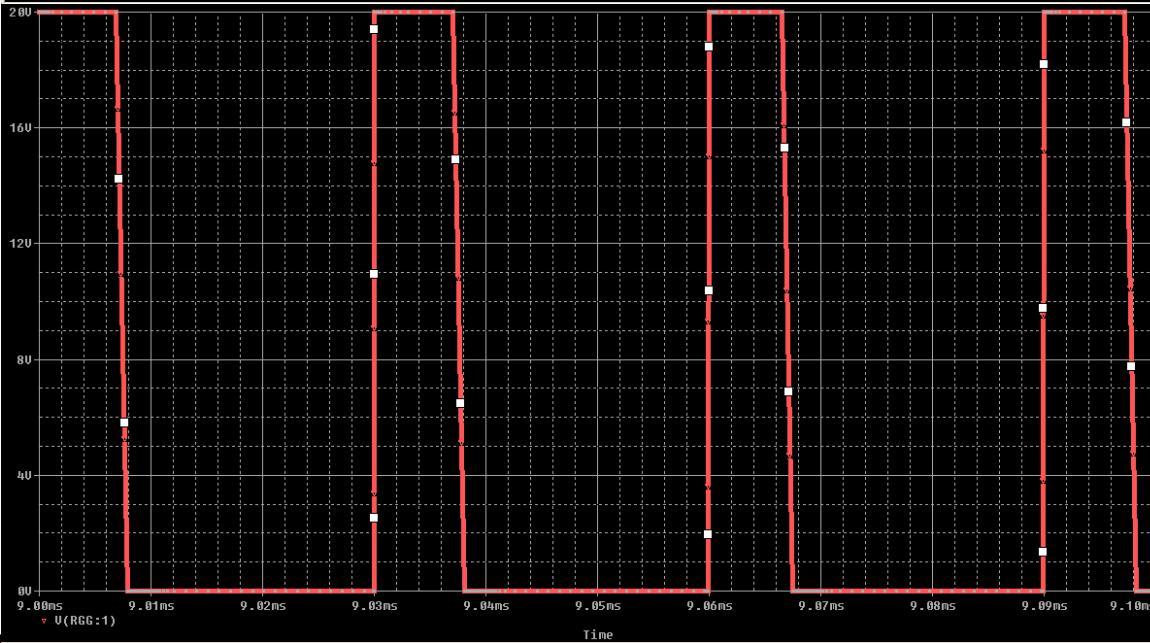


$D = 0.45$





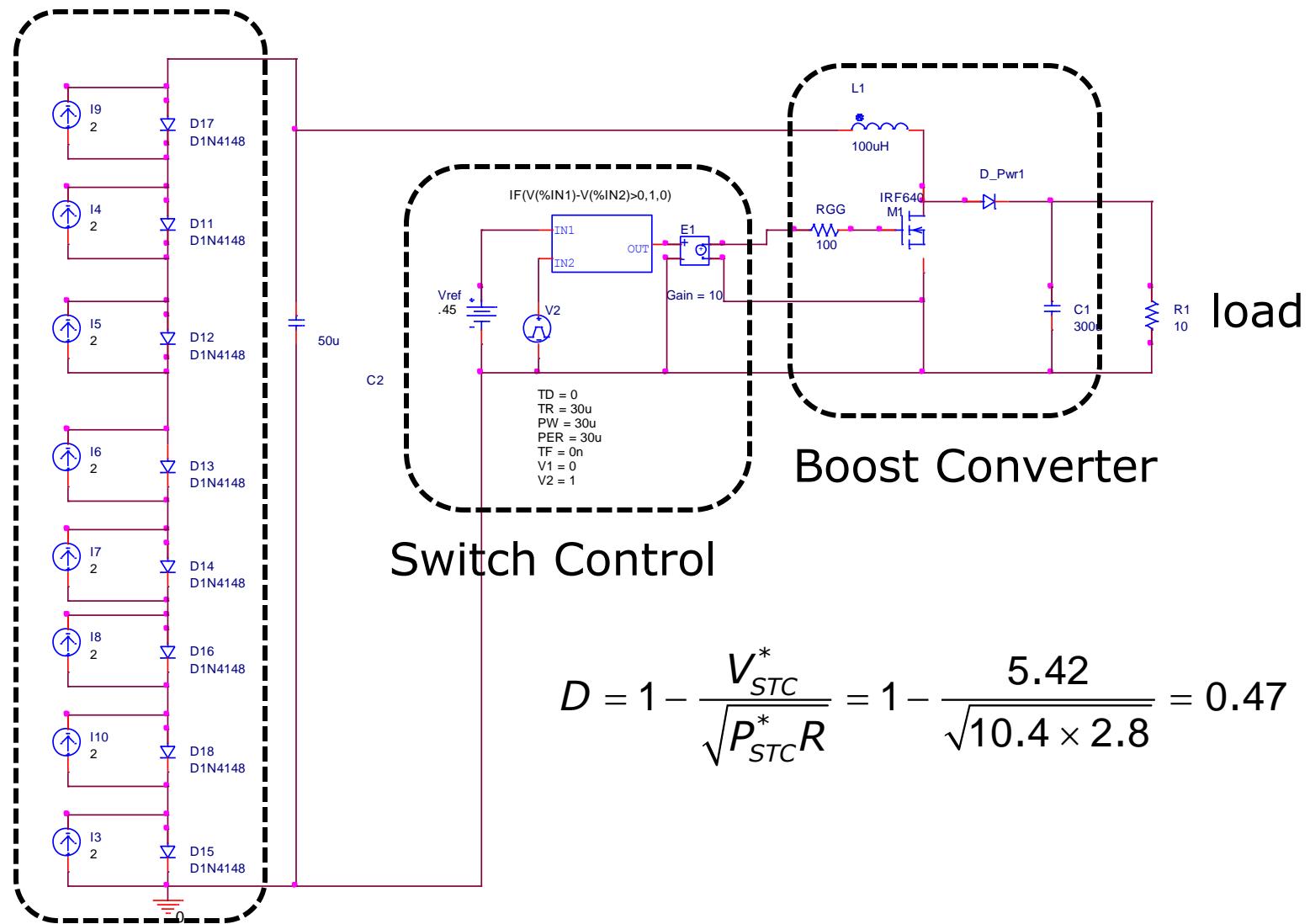
$D = 0.25$





# Maximum Power Trackers

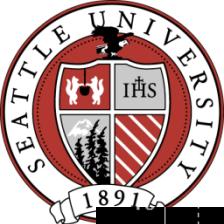
PV  
Module



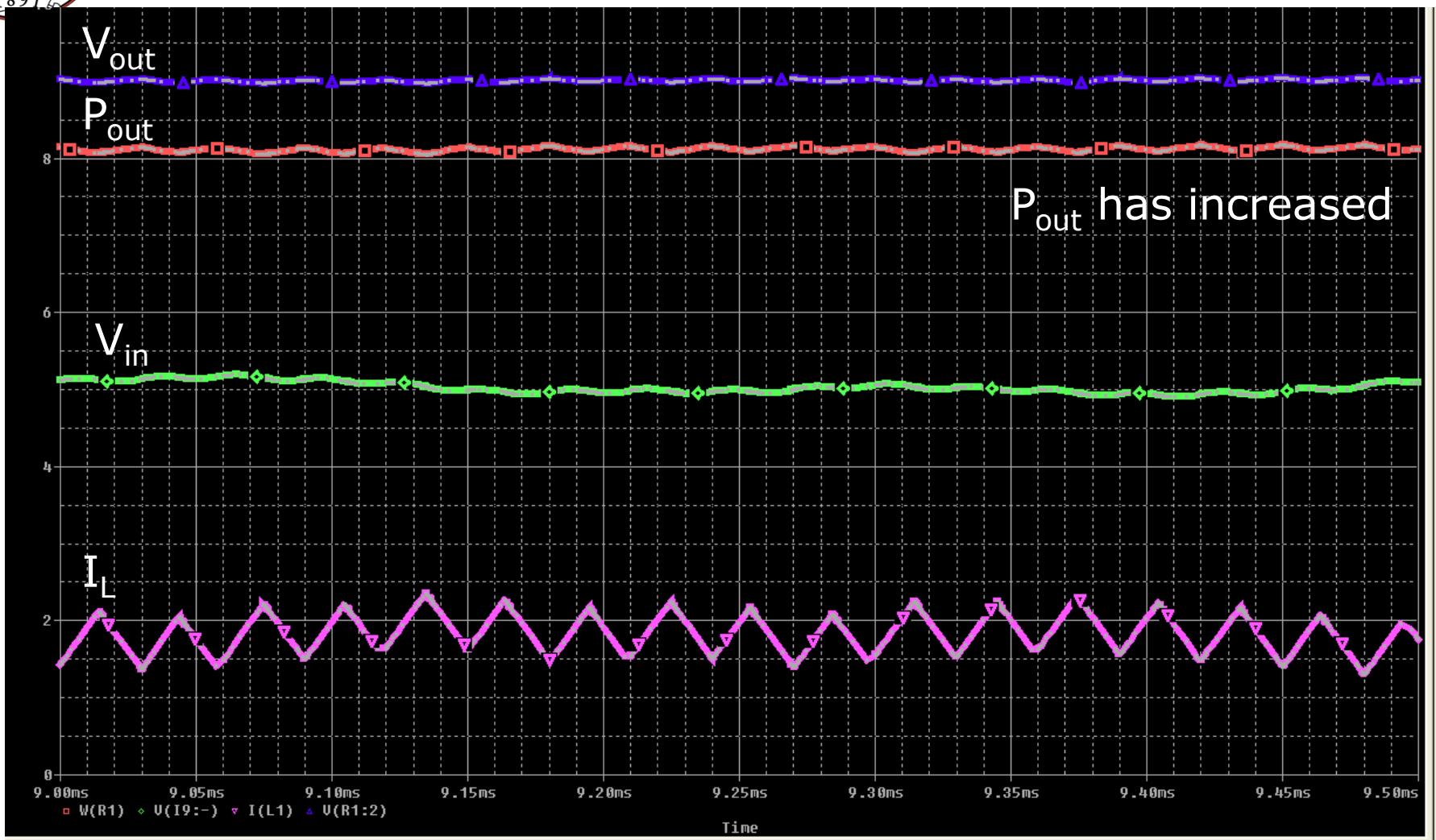


# Without MPPT





# With MPPT





## MPPT

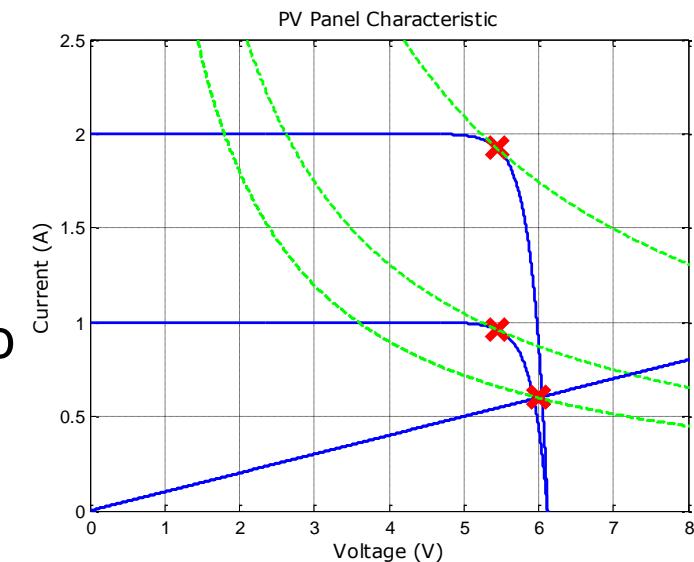
- For a given irradiance level, the optimal MPPT duty ratio is 0.45. If the irradiance decreases, how should the duty ratio be adjusted?
  - A. it should decrease
  - B. it should increase
  - C. it should stay the same



# MPPT

- For a given irradiance level, the optimal MPPT duty ratio is 0.45. If the irradiance decreases, how should the duty ratio be adjusted?
  - A. it should decrease
  - B. it should increase
  - C. it should stay the same

Input voltage is nearly constant, but output voltage must decrease, so D must decrease





# Maximum Power Point Trackers

- Maximum power tracker control requires PV voltage and current sensing to control the duty ratio
- Control aspects are beyond the scope of this class
  - ECEGR 440: Controls
  - ECEGR 424: Power Electronics



# Maximum Power Point Trackers

- Other power electronic converters may be used
  - Buck
  - Buck-Boost
  - Others
- Efficiencies in the range of 90% are possible
- MPPTs are very important for motors and pumps
  - Increases power output
  - Prolongs life